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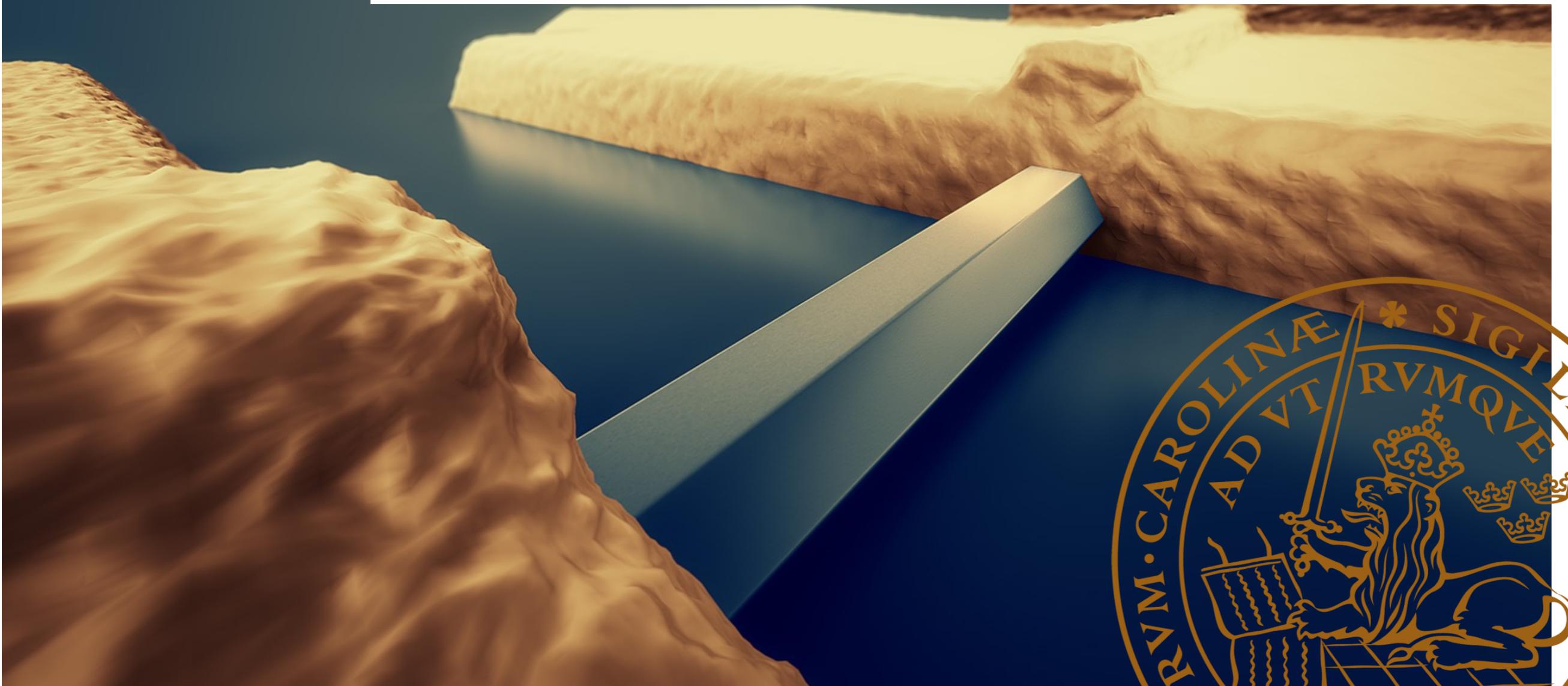
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OF NANOSCIENCE

Optimal power and efficiency of a quantum-dot heat engine

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QTD Espoo, June 25th, 2019



Outline



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- QD heat engine + motivation
- Theory & Experimental setup
- Power
- Efficiency

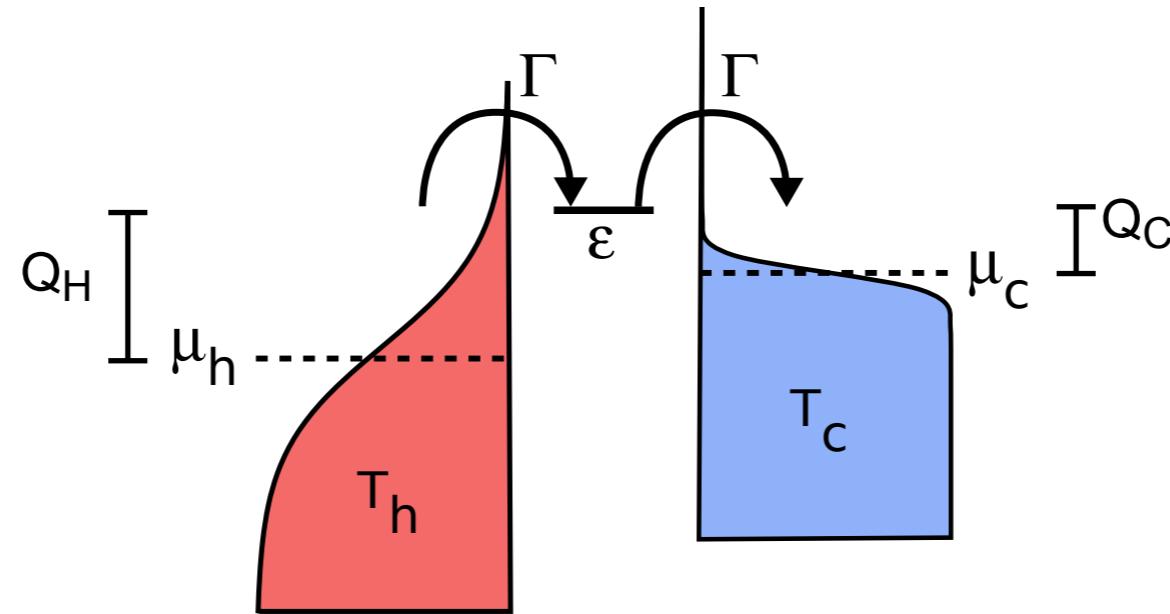
Further reading

- [M. Josefsson et al. Nature Nanotechnology 13, 920 \(2018\)](#)
[M. Josefsson et al. arXiv:1903.12618](#)

QD Heat Engine



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$$\text{Transmission} \propto \delta(E - \varepsilon)$$

Energy filtering \rightarrow net particle/energy flux

Electronic efficiency limits (QD):

Overall maximum

$$\eta_C = 1 - \frac{T_C}{T_H}$$

At maximum power

$$\eta_{CA} = 1 - \sqrt{\frac{T_C}{T_H}} \approx \frac{\eta_C}{2}$$

Experiments

The QD

InP-segment in a InAs nanowire

Band-gap offset confines electrons

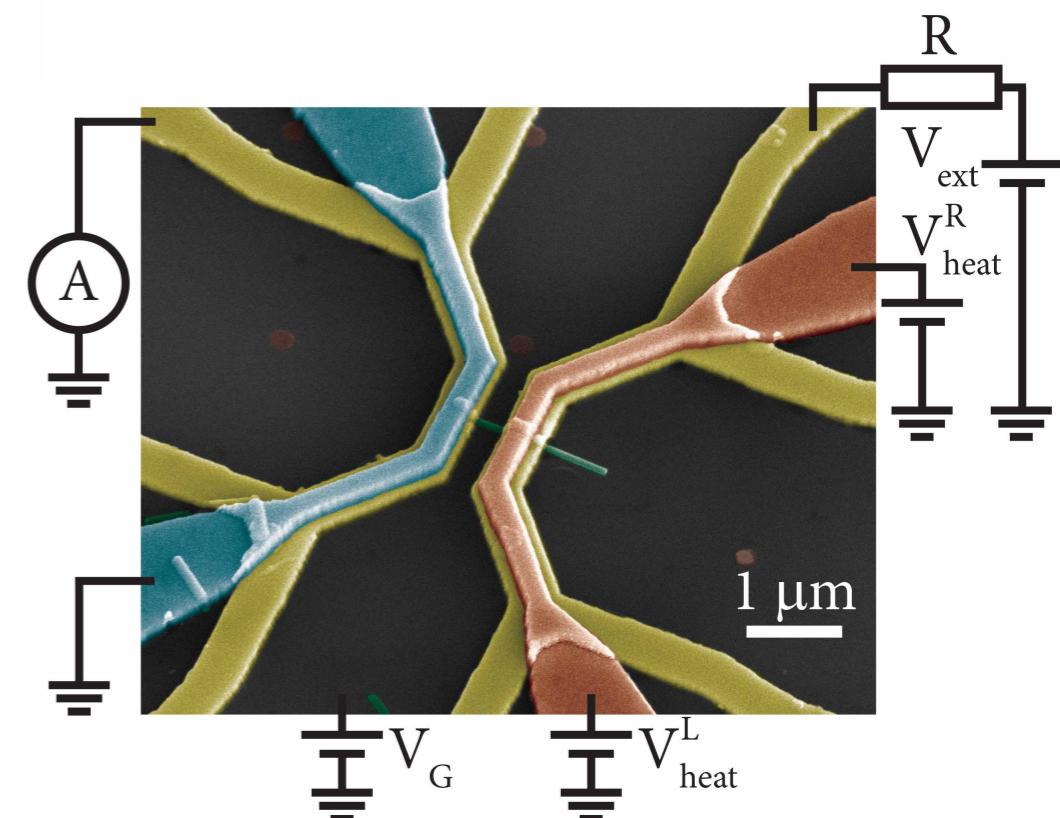
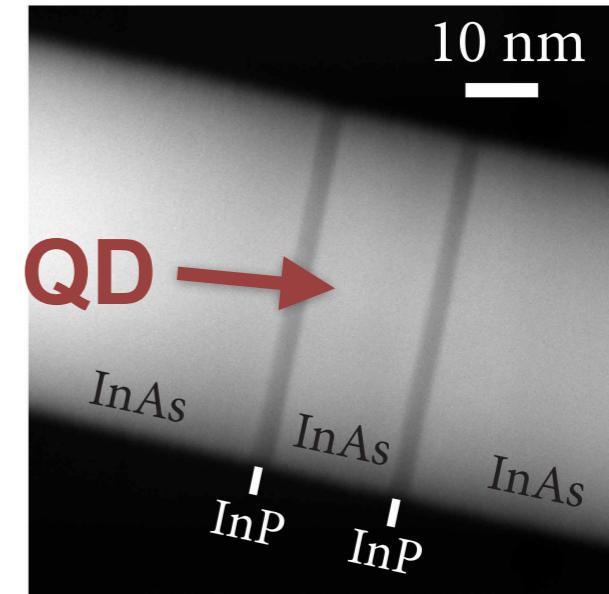
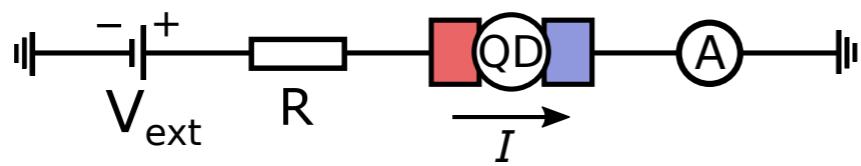
Circuitry

Metallic contacts

"Top-heaters" used for thermal biasing

$\Delta T = T_H - T_C$ and/or V_{ext} generates a current

External load R



Theory

$$\eta = \frac{P}{J_Q}$$

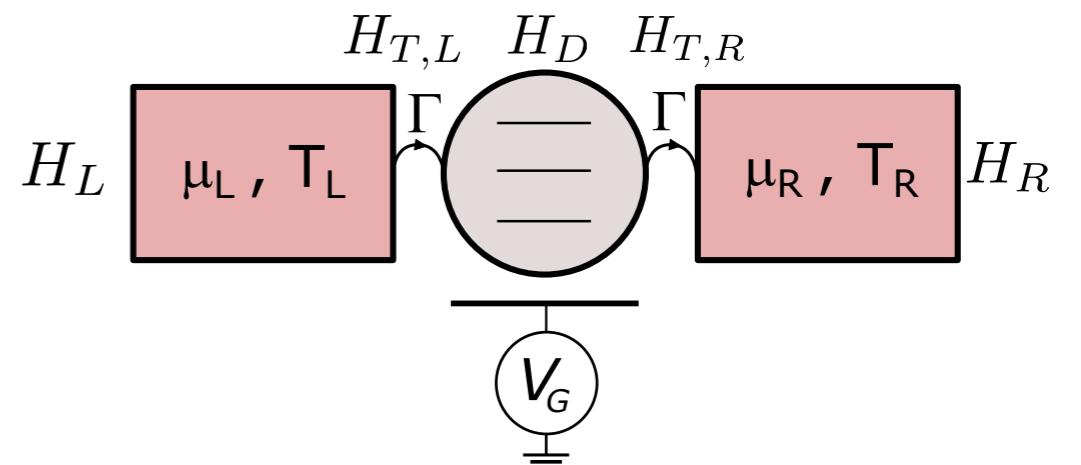
Measured

Calculated

Anderson model

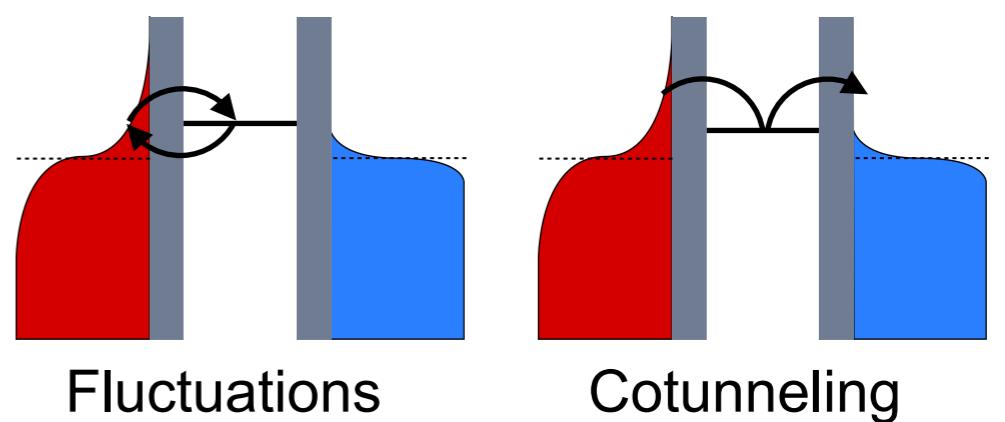
- Small Γ , large e-e interactions

$$H = H_D + \sum_r H_r + \sum_r T_{T,r}$$



Real-time diagrammatics

- Master equations
- Keep terms up to Γ^2
 - Charge current
 - Heat current (no phonons)





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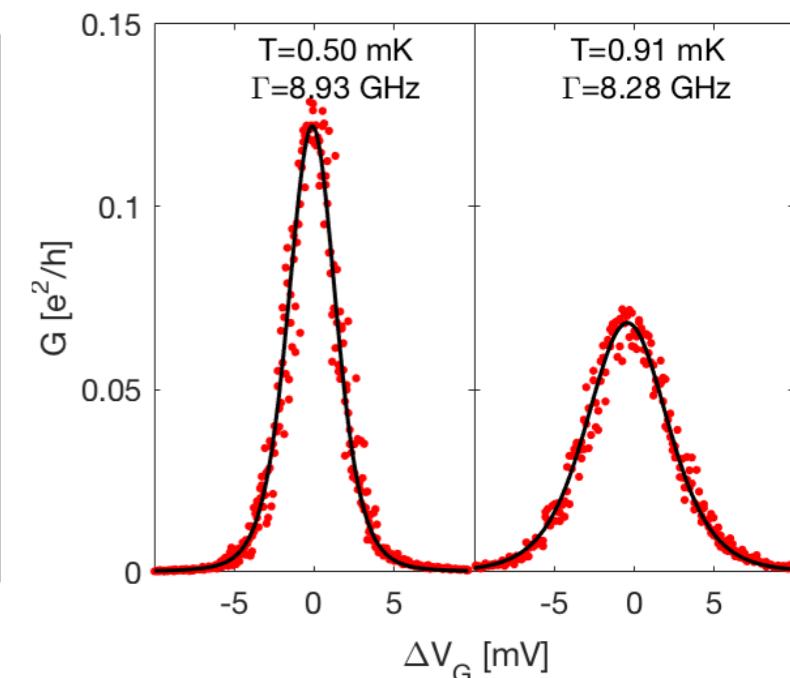
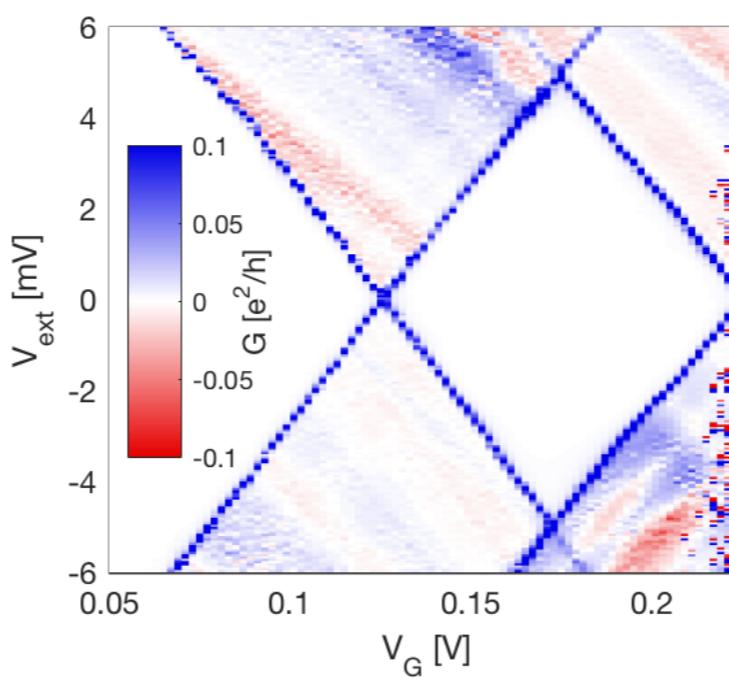
Conductance and power

Device characterization

Conductance ($\Delta T = 0$):

E_C and α from stability diagram

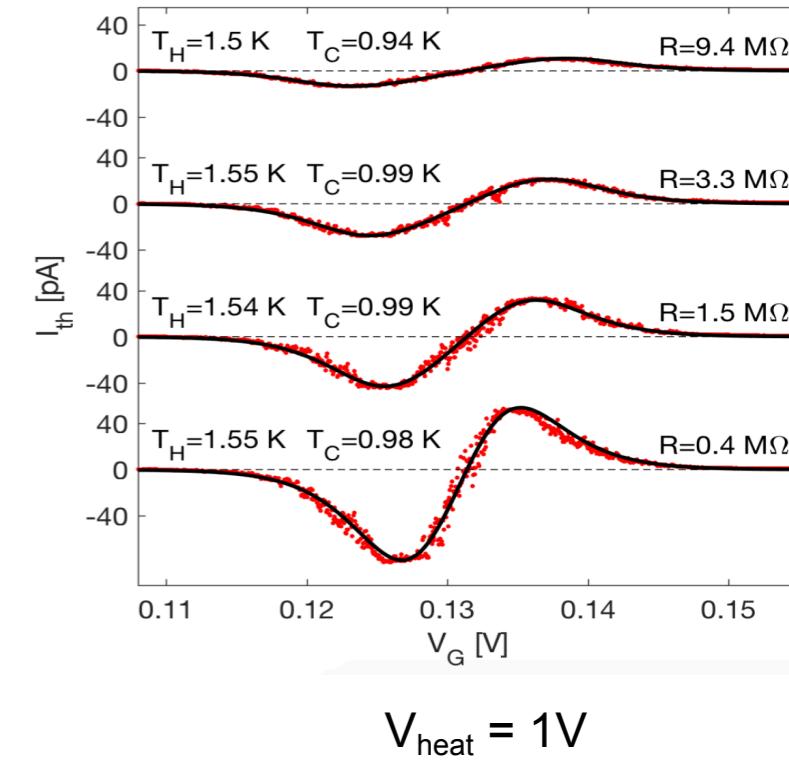
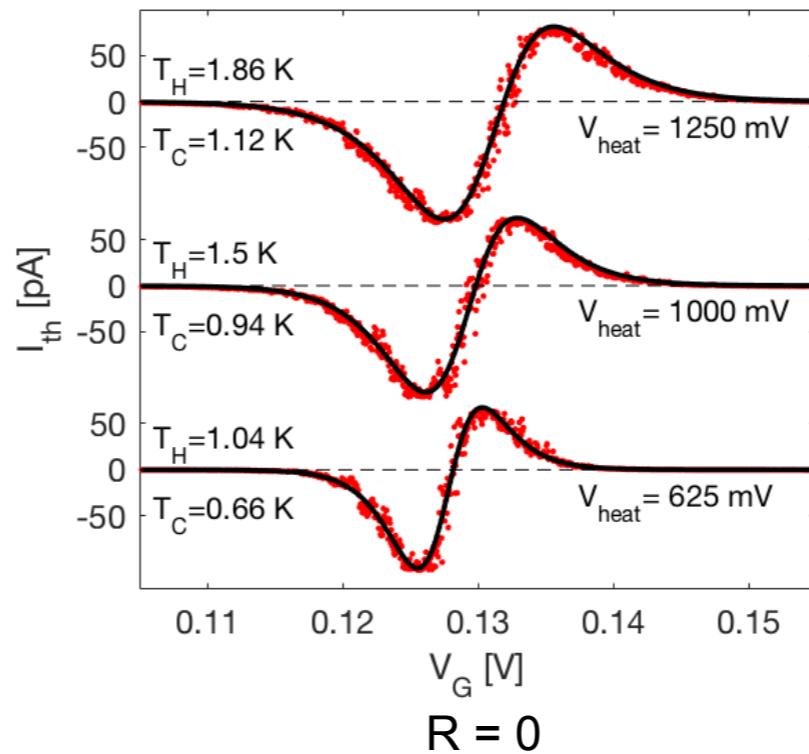
Γ from $G(V_G)$ (fit)



Thermocurrent ($\Delta T > 0$):

T_H and T_C from $I(V_G)$ (fit)

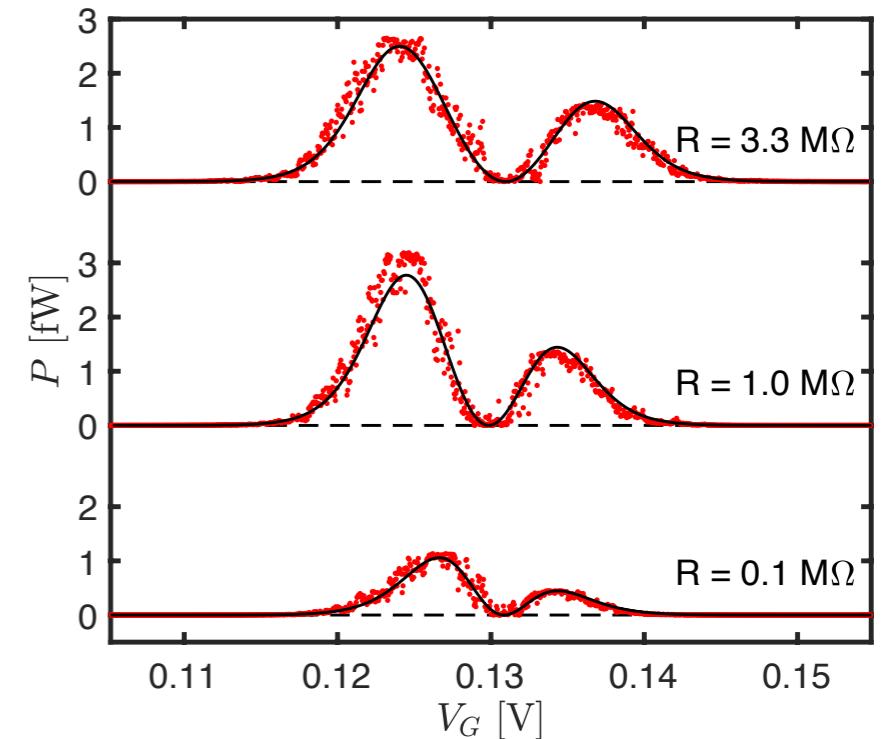
Repeated for each $I(V_G)$



Power & Load Matching 1

Remove V_{ext} - attach load.

Only power generation $P > 0$

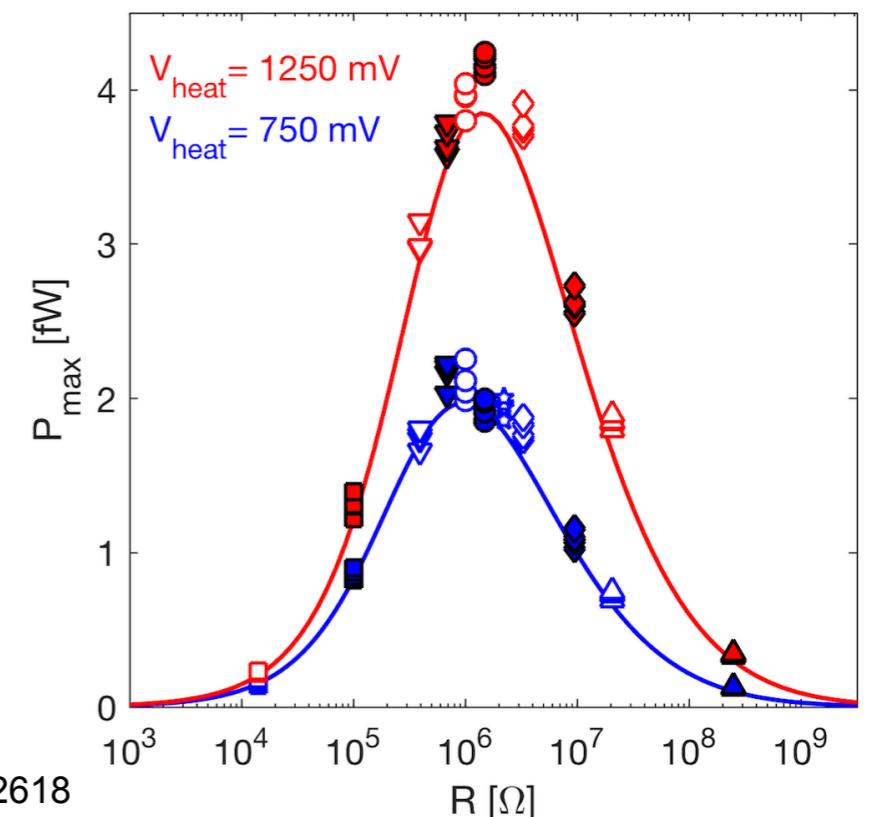


Optimal load (theory)

Linear response and sequential tunneling

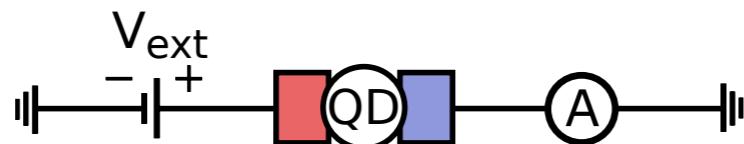
$$R_P \approx 2.507 \frac{k_B(T_H + T_C)}{2\hbar\Gamma} \frac{h}{e^2}$$

Non-linear and second order effects: $\sim 1\%$



Power 2

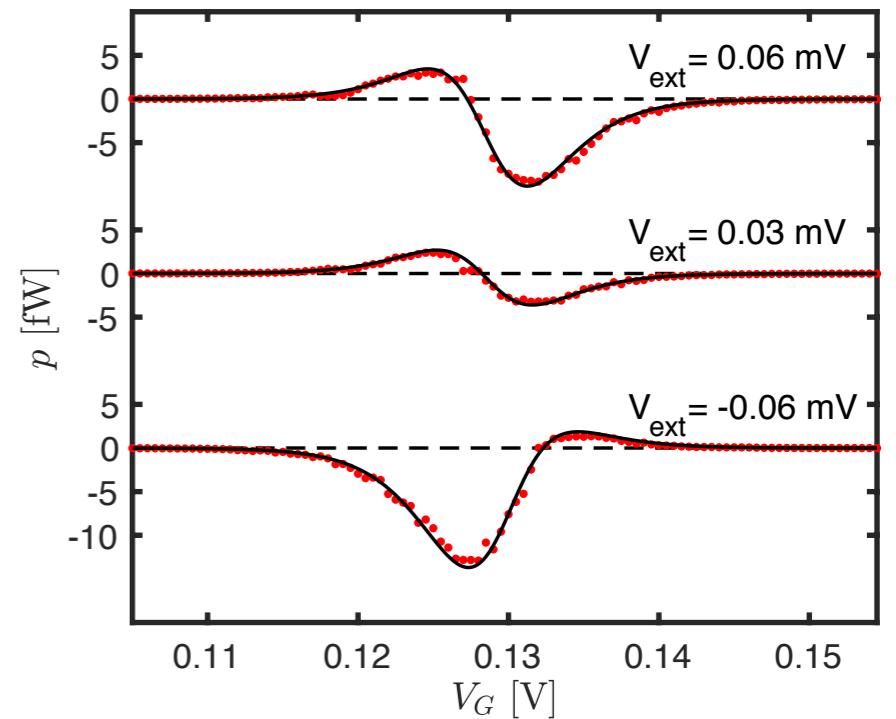
Use V_{ext} to simulate a load: $P = -IV_{ext}$



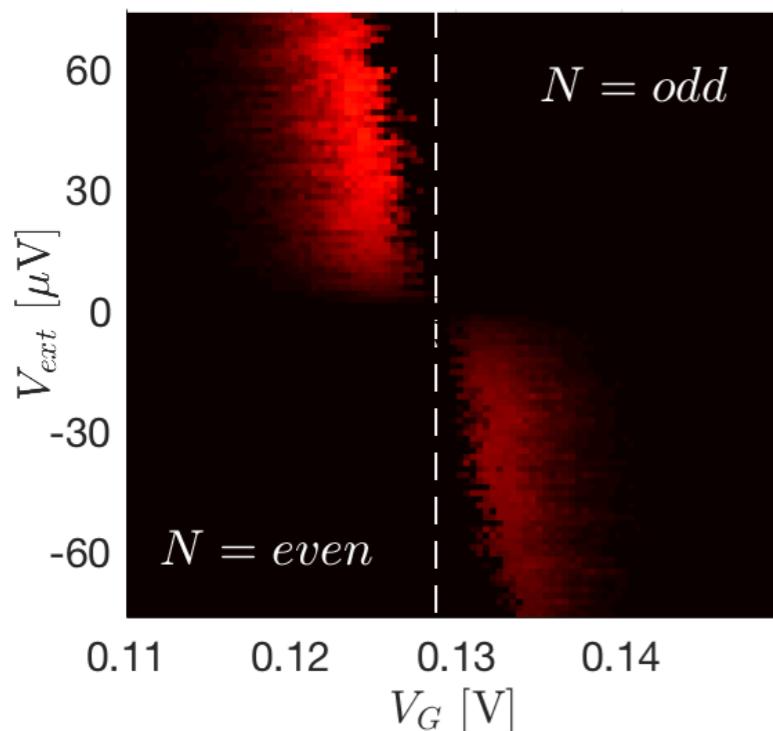
Two modes of operation:

$P > 0$ generator

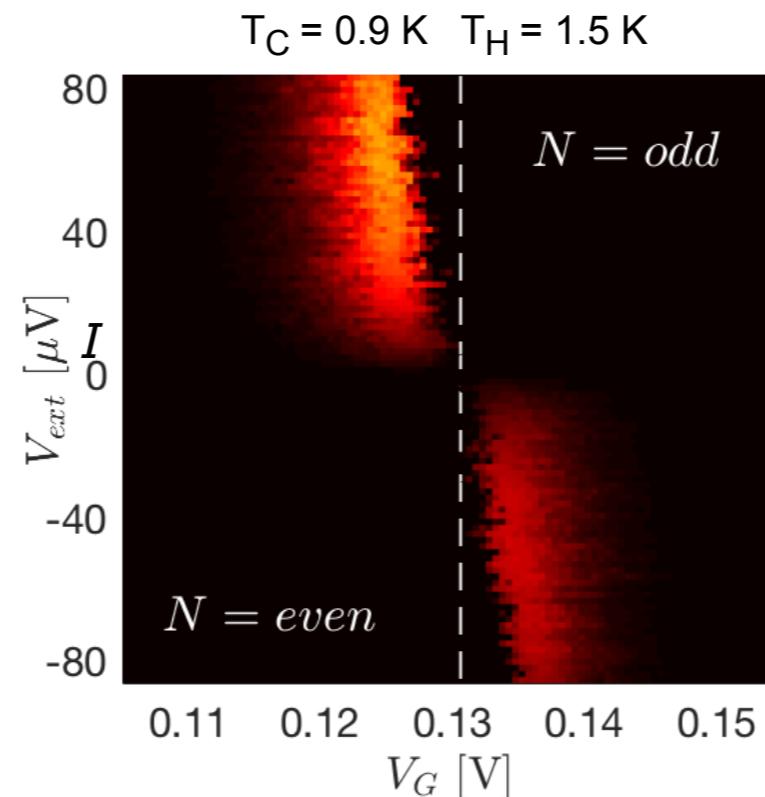
$P < 0$ refrigerator



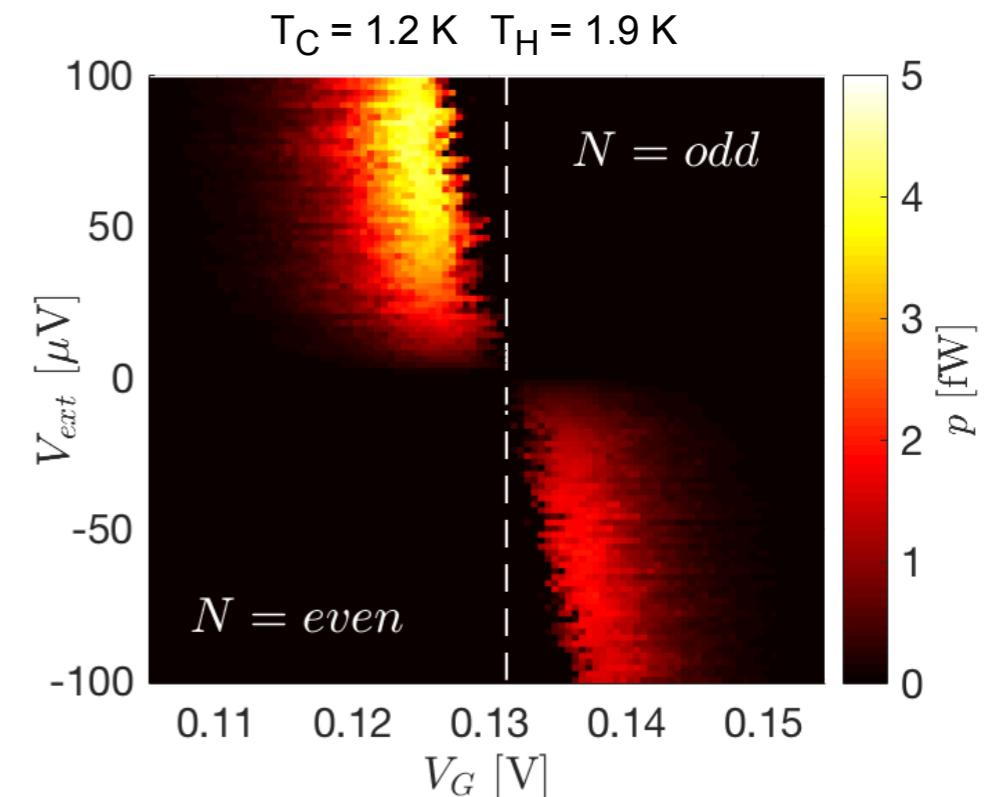
$T_C = 0.75$ K $T_H = 1.2$ K



$T_C = 0.9$ K $T_H = 1.5$ K

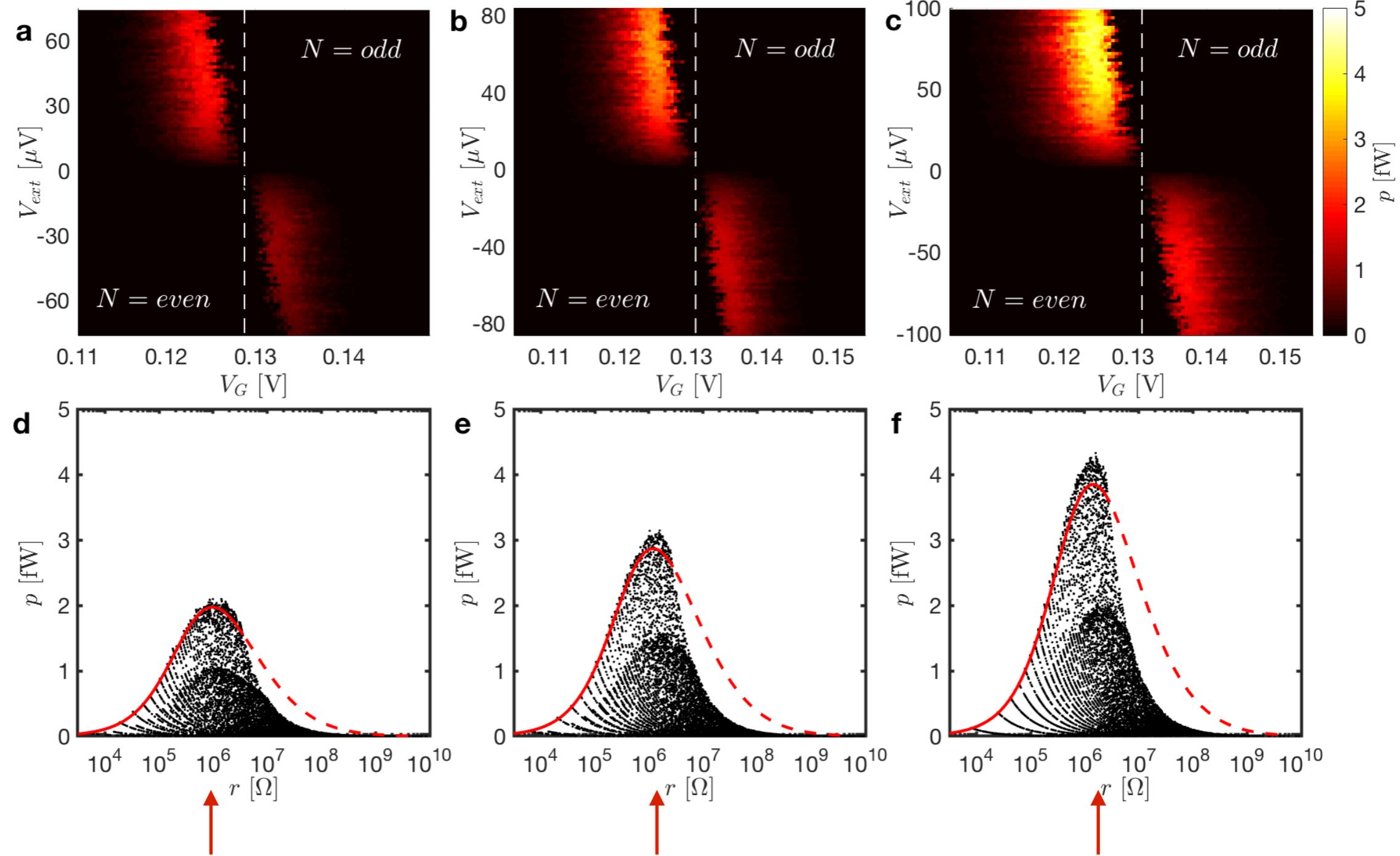


$T_C = 1.2$ K $T_H = 1.9$ K



Load Matching 2

Find optimal load from P vs I/V_{ext}





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Efficiency

Efficiency

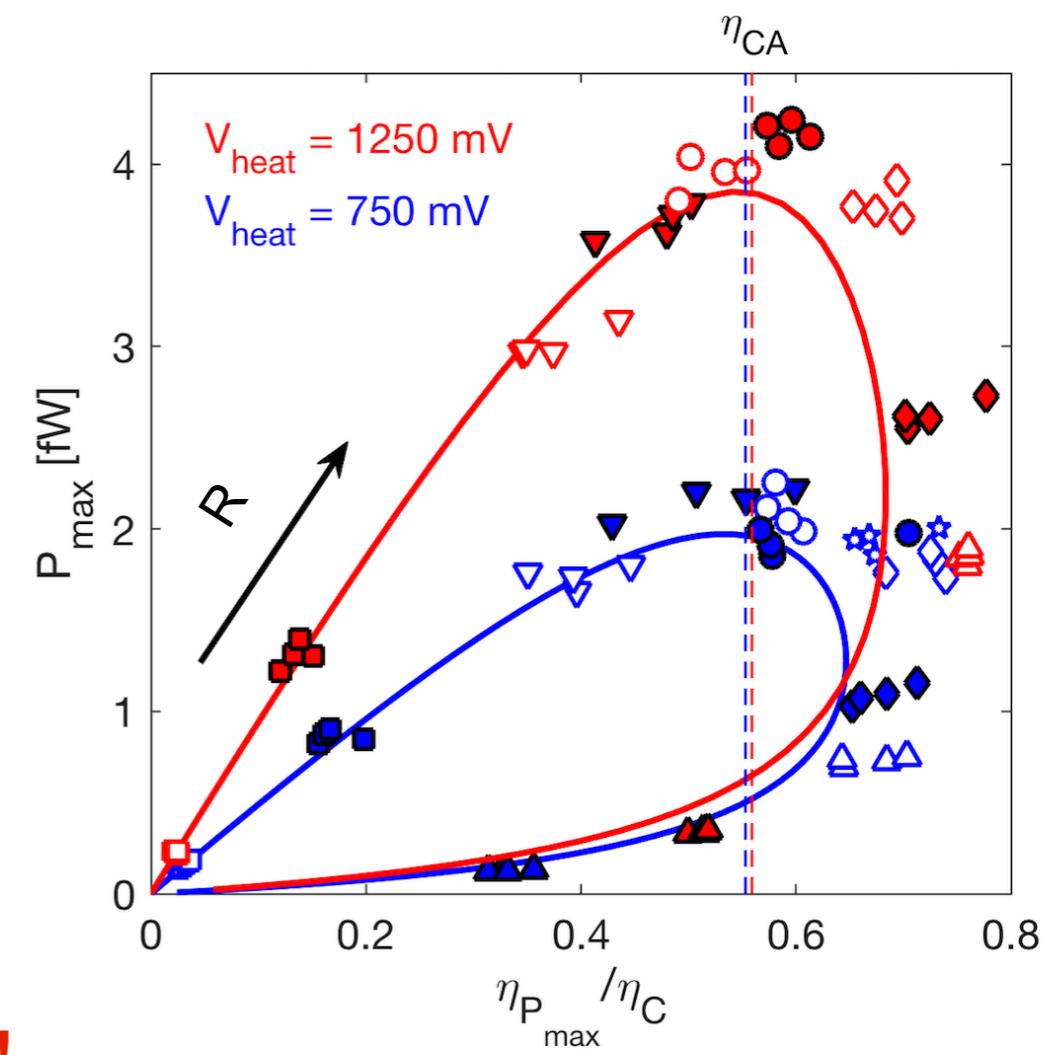
Our device

Focus on V_G optimized for P

Curzon-Ahlborn efficiency η_{CA} at maximum P

$\eta \sim 0.7\eta_C$ at $P=50\%$ of max P

First high efficiency estimates in a real device!



$$\eta = \frac{P}{J_Q}$$

Measured

Calculated

Efficiency - second order

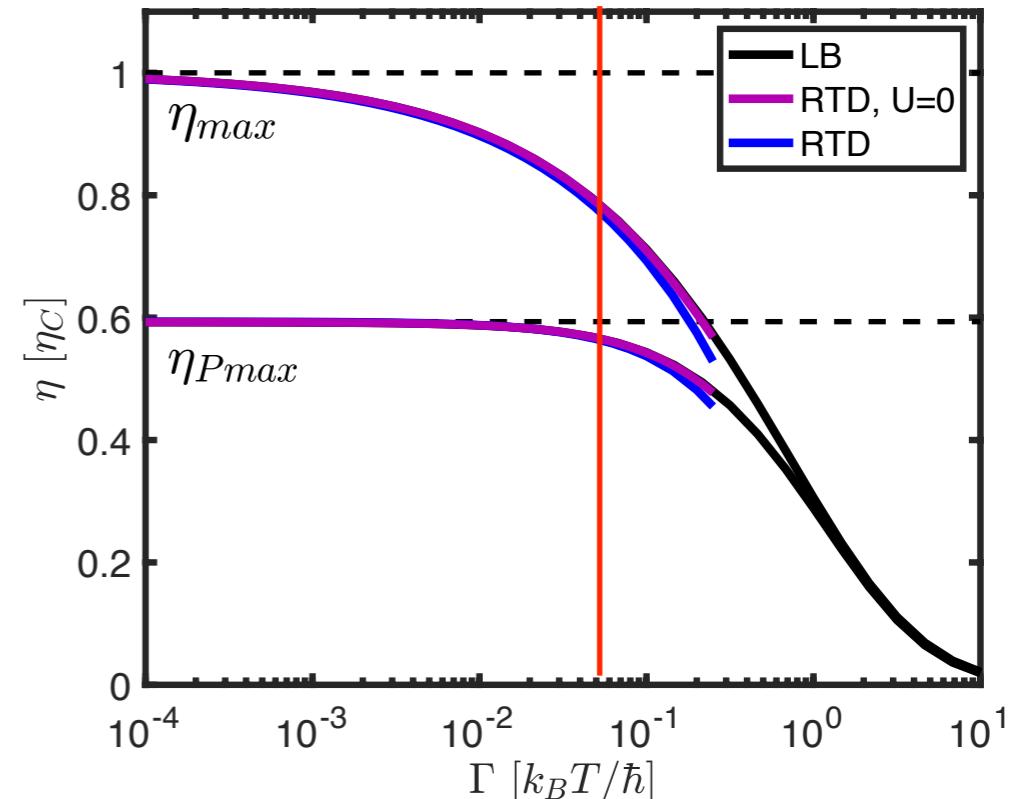
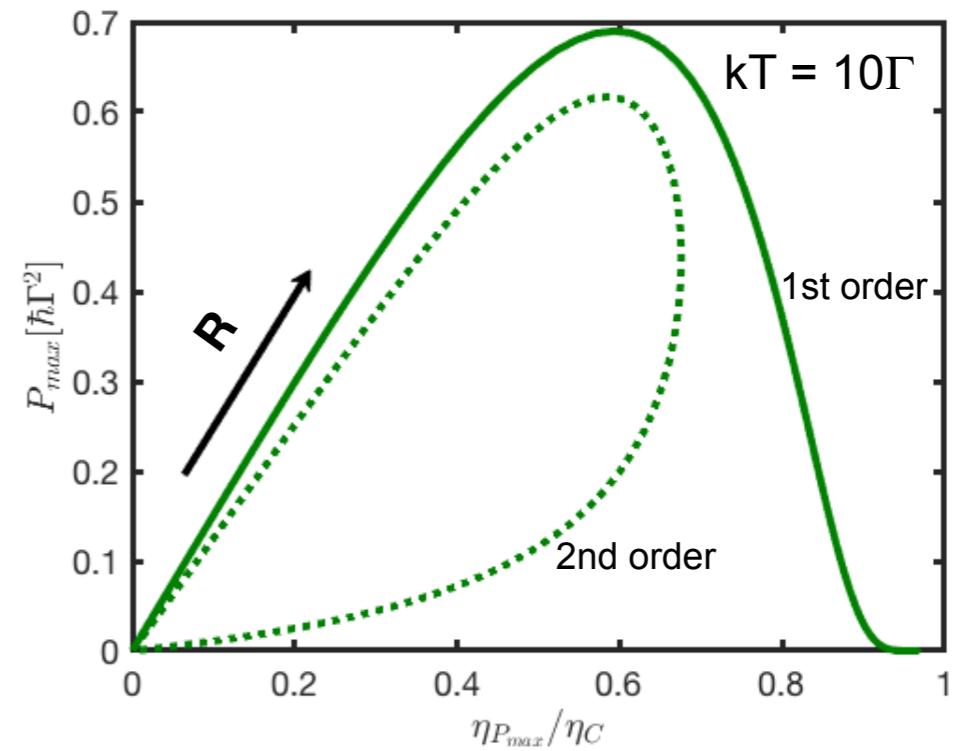
General anderson QDs

Second order effects - broadening

Max η for our device 70-80% of η_C

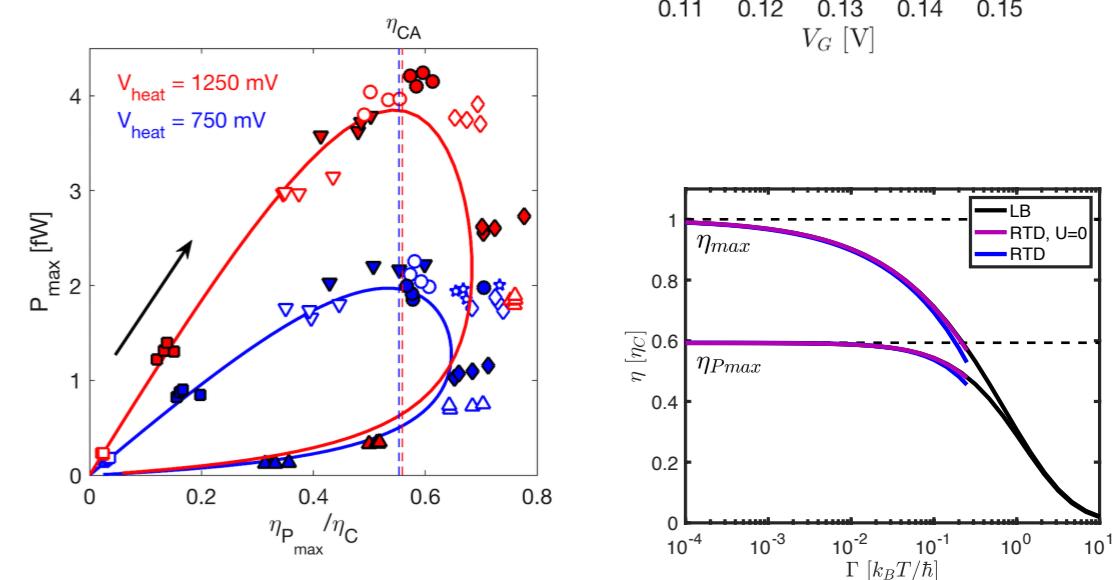
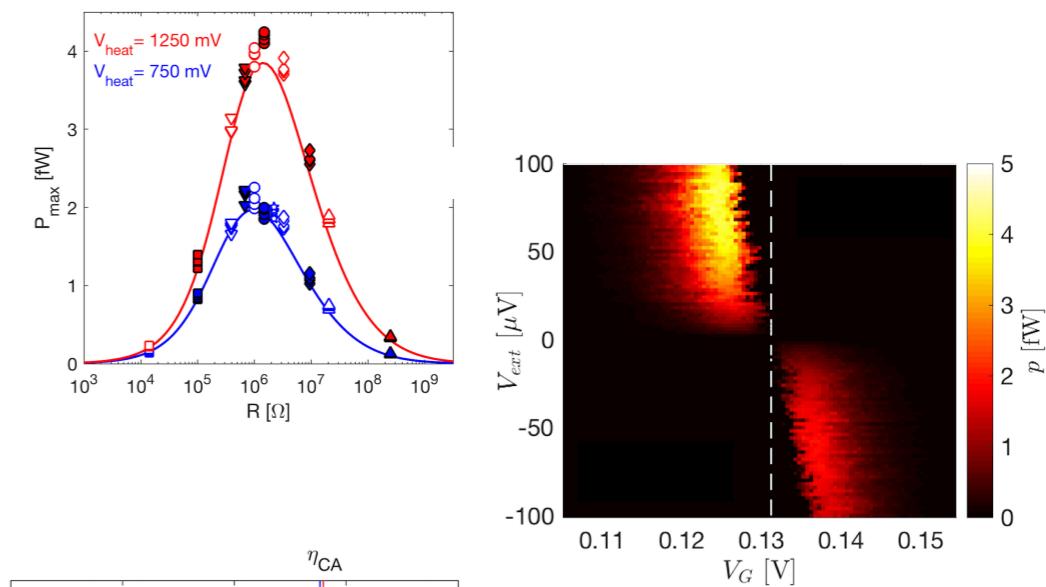
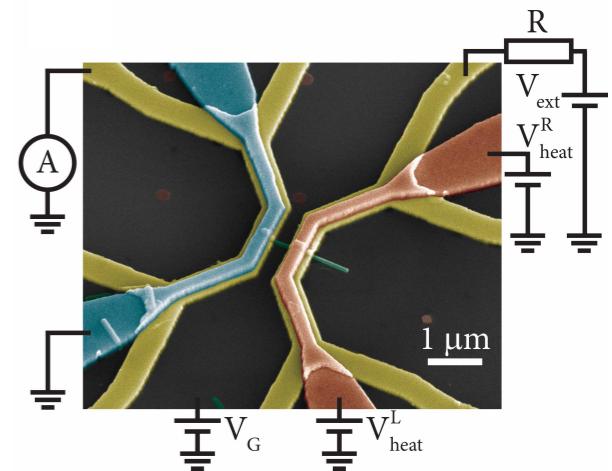
η at max P less sensitive

Second order effects important!



Summary

- Theory and experiments on a single QD heat engine
- Load matching - several options
- $\eta = \eta_{CA}$ when R is optimized for high power
- $\eta \sim 0.7\eta_C$ when R is optimized for high power
- Second order tunneling important for η





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